



in the “Real World”

How does it work? | Modal Model

Modes are used to represent **perturbations** to a perfect beam

Represent the beam with different spatial basis functions by a series expansion:

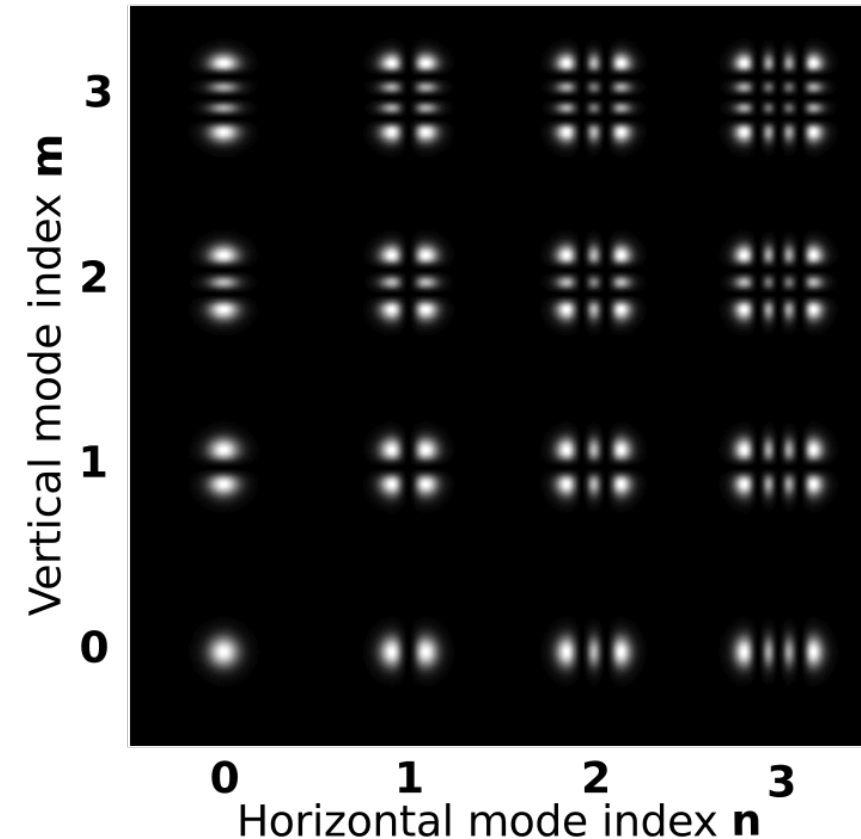
$$E(t, x, y, z) = \sum_j \sum_{n,m} a_{jnm} u_{nm}(x, y, z) \exp(i(\omega_j t - k_j z))$$

is our basis function choice, typically we use

Hermite-Gauss (HG) modes: Rectangular symmetric

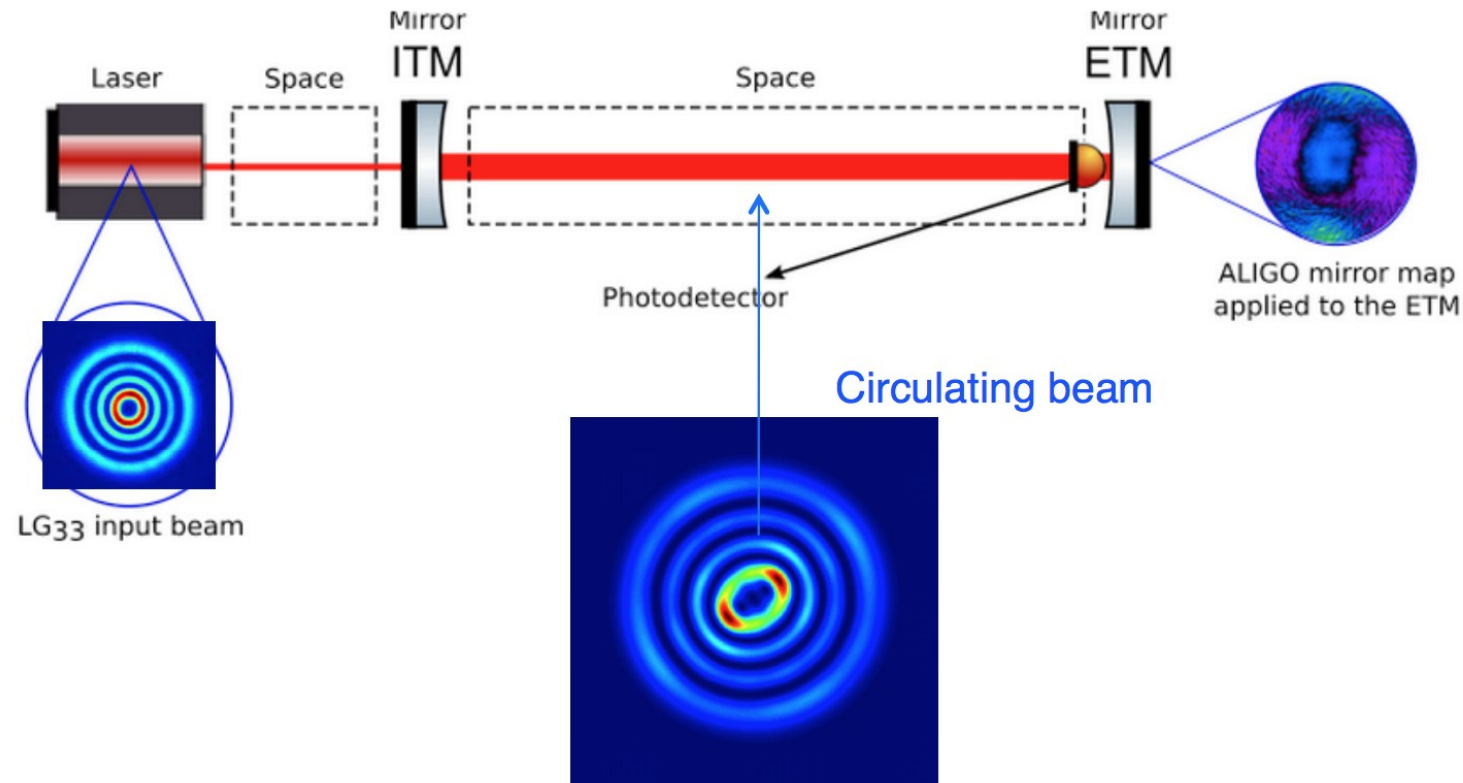
Laguerre-Gauss (LG) modes: Cylindrically symmetric

Modal model only deals with paraxial beams and small distortions, what we would expect in our optical systems.



Example: Mirror maps with LG33 mode

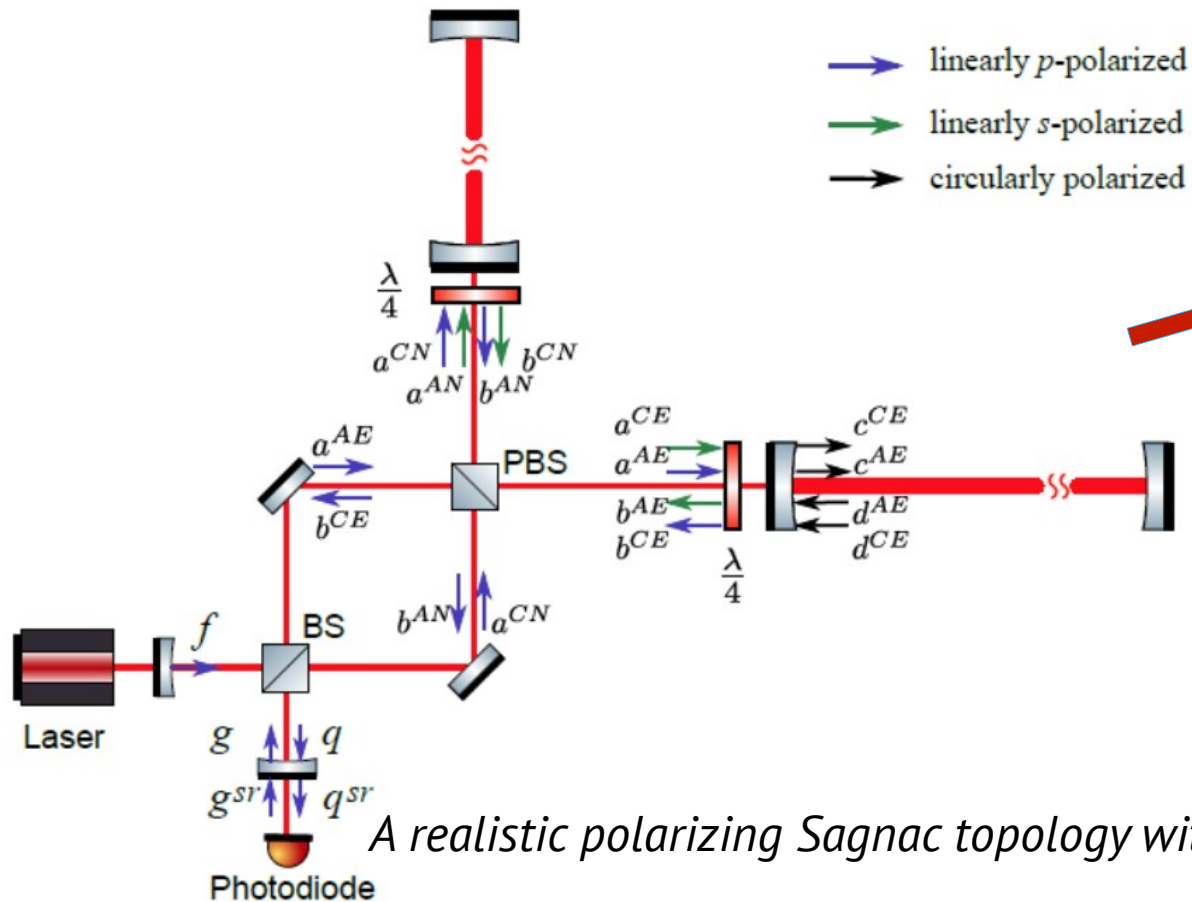
You can...Study mode purity and degeneracy in a cavity with realistic mirrors



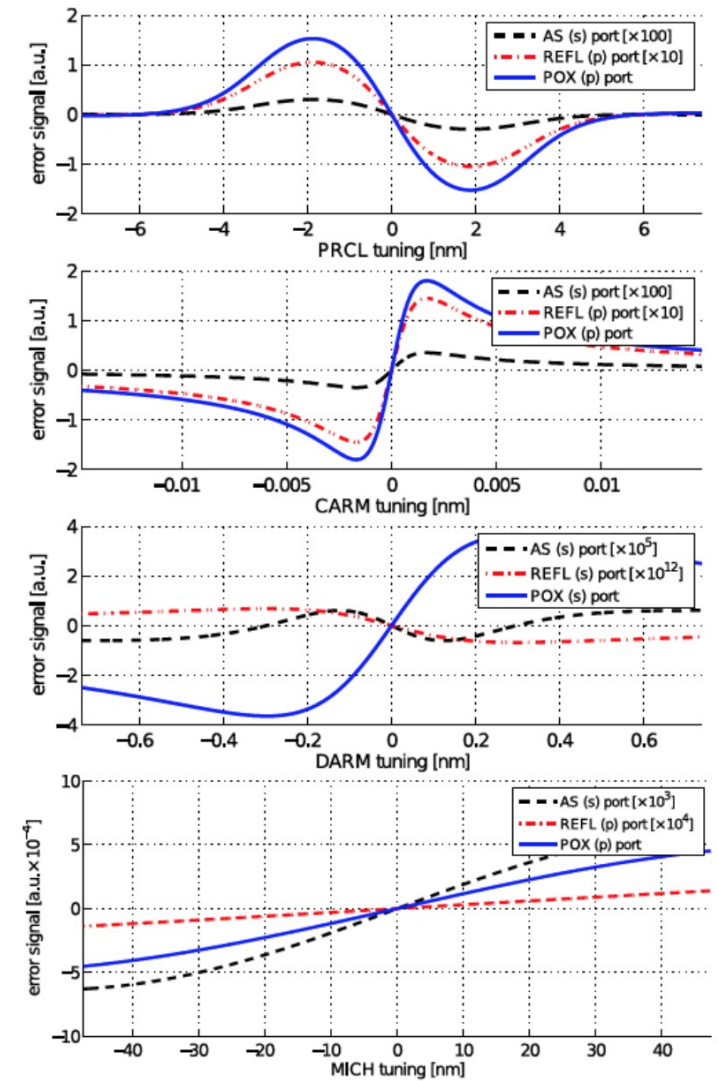
Higher order Laguerre-Gauss mode degeneracy in realistic, high finesse cavities, C. Bond et. al. (2011)
arxiv.org/abs/1107.3812

Example: RF Control Signals

You can...Calculate length control signals for a new interferometer topology

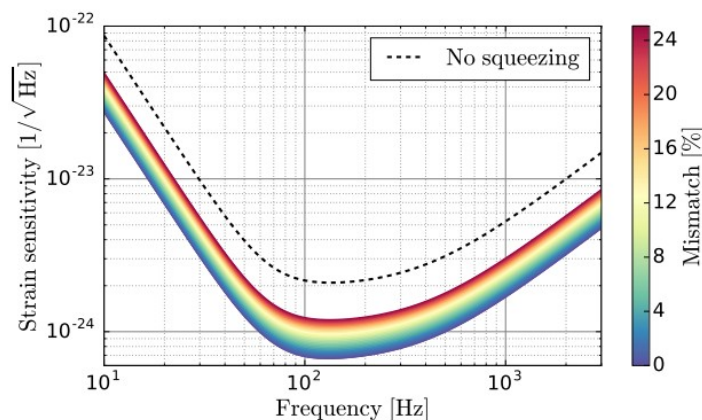
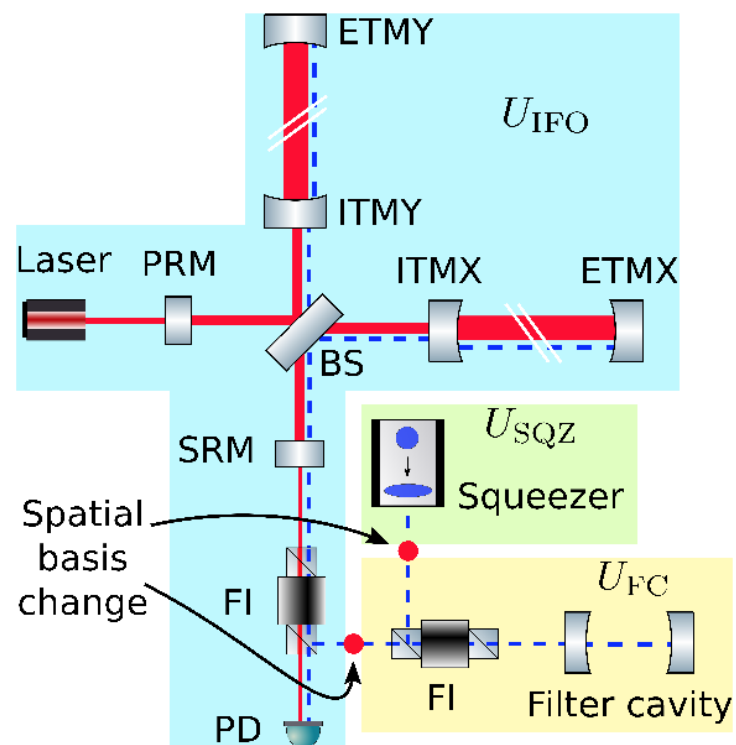


A realistic polarizing Sagnac topology with DC readout for the Einstein Telescope M.Wang et. al. (2013)
arxiv.org/abs/1303.5236

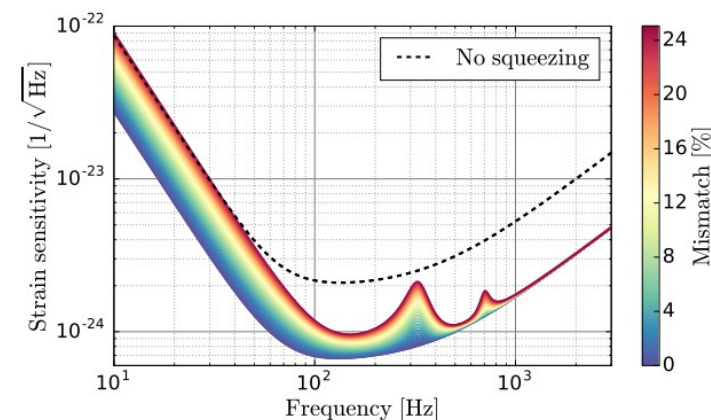


Example: Multimode Squeezing

You can...Design a new frequency-dependent squeezing scheme which is more robust to mode mismatch



Squeezer matched to filter cavity, filter cavity mismatched to IFO



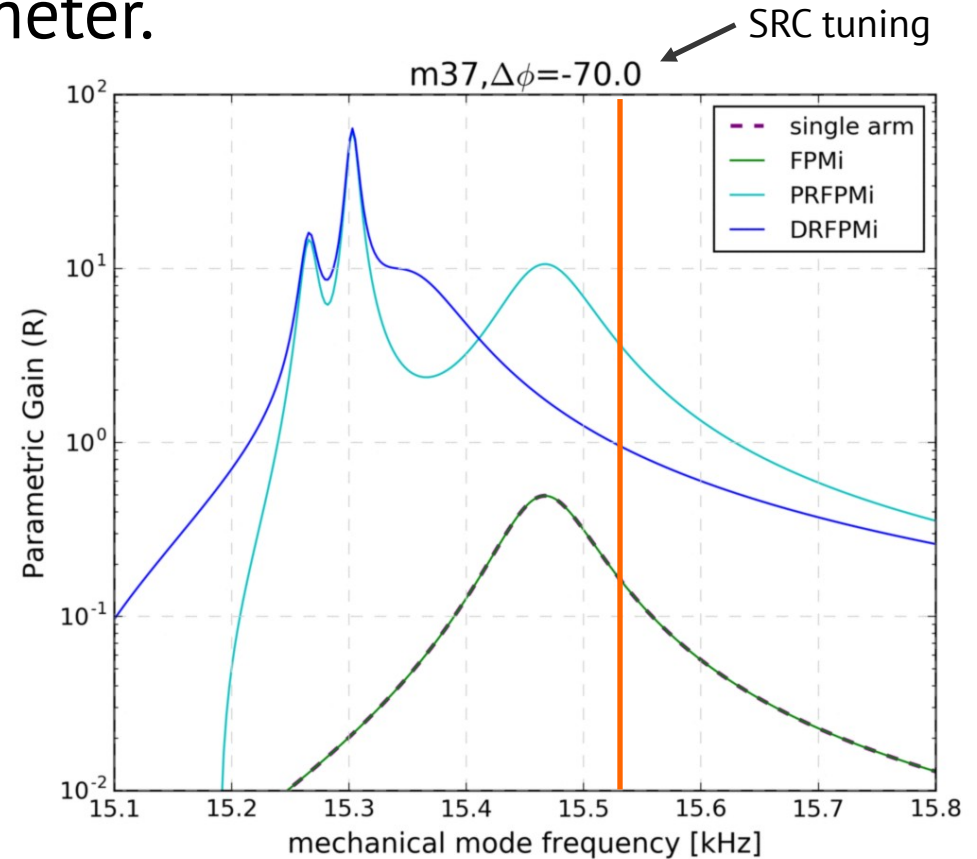
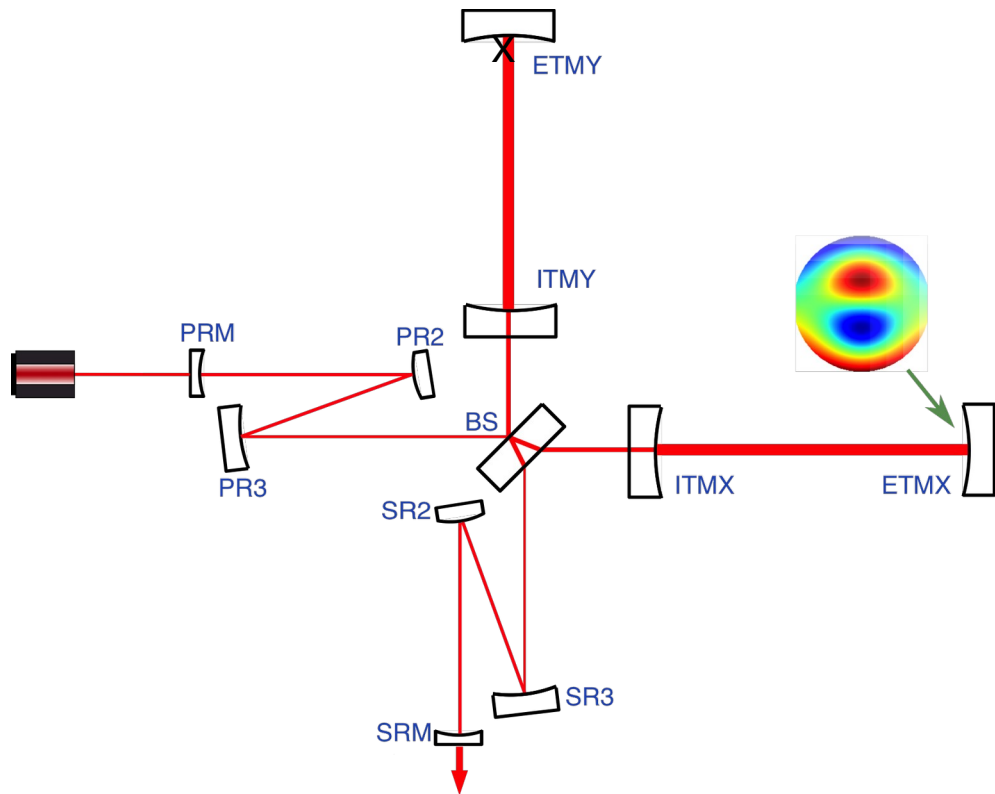
Squeezer matched to IFO, filter cavity mismatched to IFO

Multi-spatial-mode effects in squeezed-light-enhanced interferometric gravitational wave detectors

D. Töyrä et. al. (2017) arxiv.org/abs/1704.08237

Example: Parametric Instabilities

You can... Show how higher order radiation pressure effects are affected by the topology of the interferometer.



The Influence of Dual-Recycling on Parametric Instabilities at Advanced LIGO, A. Green et. al. (2017)

arxiv.org/abs/1704.08595

Example: Coupled Cavity Effects

You can... Highlight problems in analytical assumptions for future detectors.

